

# On two-phase flow models for Coriolis flowmeters

Xiao-Zhang ZHANG

*Tsinghua University, Beijing, P R China*

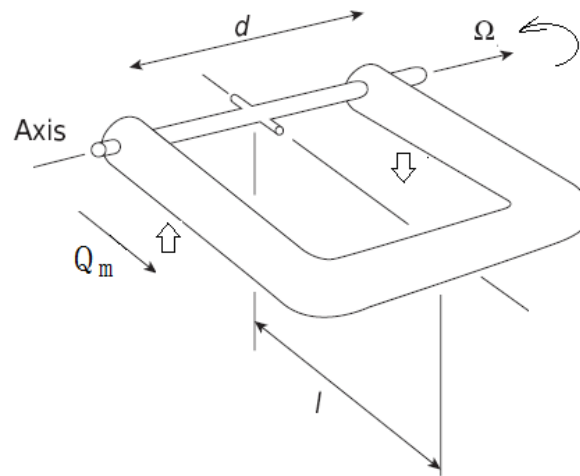
*E-mail: zhangxzh@tsinghua.edu.cn*

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# Introduction

- a Coriolis flowmeter measures flowrate by force.
- play as a 'real' mass flowmeter.
- multi-purpose measurement by one meter.



Based on Baker: Flow Measurement Handbook, 2<sup>nd</sup> Ed. CUP

# Errors of Coriolis flowmeters in multiphase flow (Test data)

Author	Coriolis meter installation	Fluids	Void fraction	Max. Error
Skea and Hall	Straight, Curved	Oil+N <sub>2</sub>  Water in oil, Oil in water	6% N <sub>2</sub> 9% N <sub>2</sub> Max. 15%	-15% +5% 0.3%(small)
	3 others			Not work
Wang et al	Vertical	Liquid and gas CO <sub>2</sub>	0~70%	-16%~2%
	Horizontal			-4%~14%
Michael et al	normal	High viscous oil N <sub>2</sub>	0~90%	±2%
				±5%
Liu et al	U type	air, water	0~35%	0~-25%
B B Tao et al	U type, horizontal	Gas, water	0~25%	2%~-22%
Weinstein	U type, up/down	Gas, water	0~8%	Up: -15%, down: 12%

## Models for Coriolis flowmeters in multiphase flow

- 2003 Hemp and Hoi: bubble model – solid sphere
- 2006 Hemp and Kutin: compressibility, well mixed
- 2007 Gysling: aeroelastic model
- 2008 Weistain Ph D thesis: phase decouple , relative speed
- 2014 Wang and Baker: detailed Review of Coriolis flowmeter
- 2016 Basse: damping
  
- 2001 Liu at el: neural network for signal

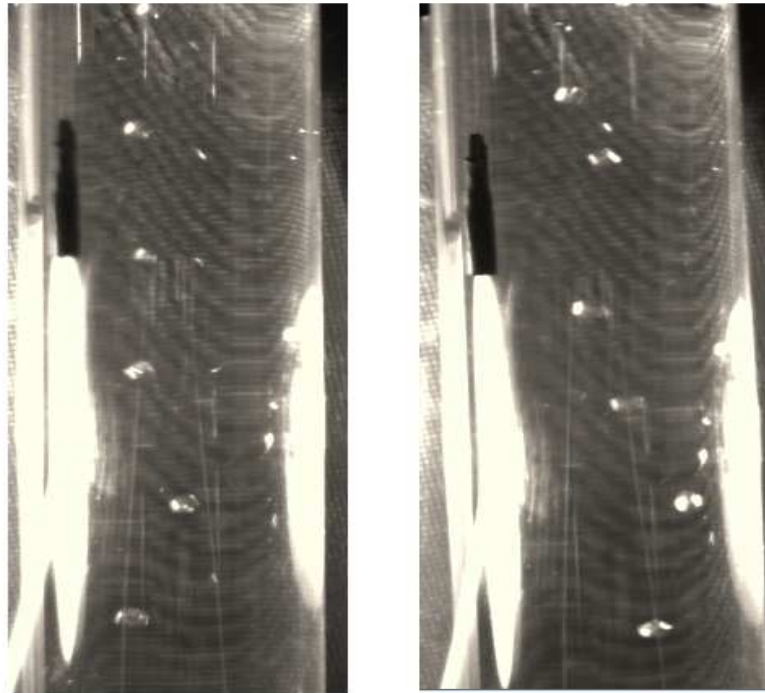
But works still being done to improve the models

we were trying to look at how multiphase  
flows affect a Coriolis flowmeter

# Experiment -1 : Bubble rising in still water

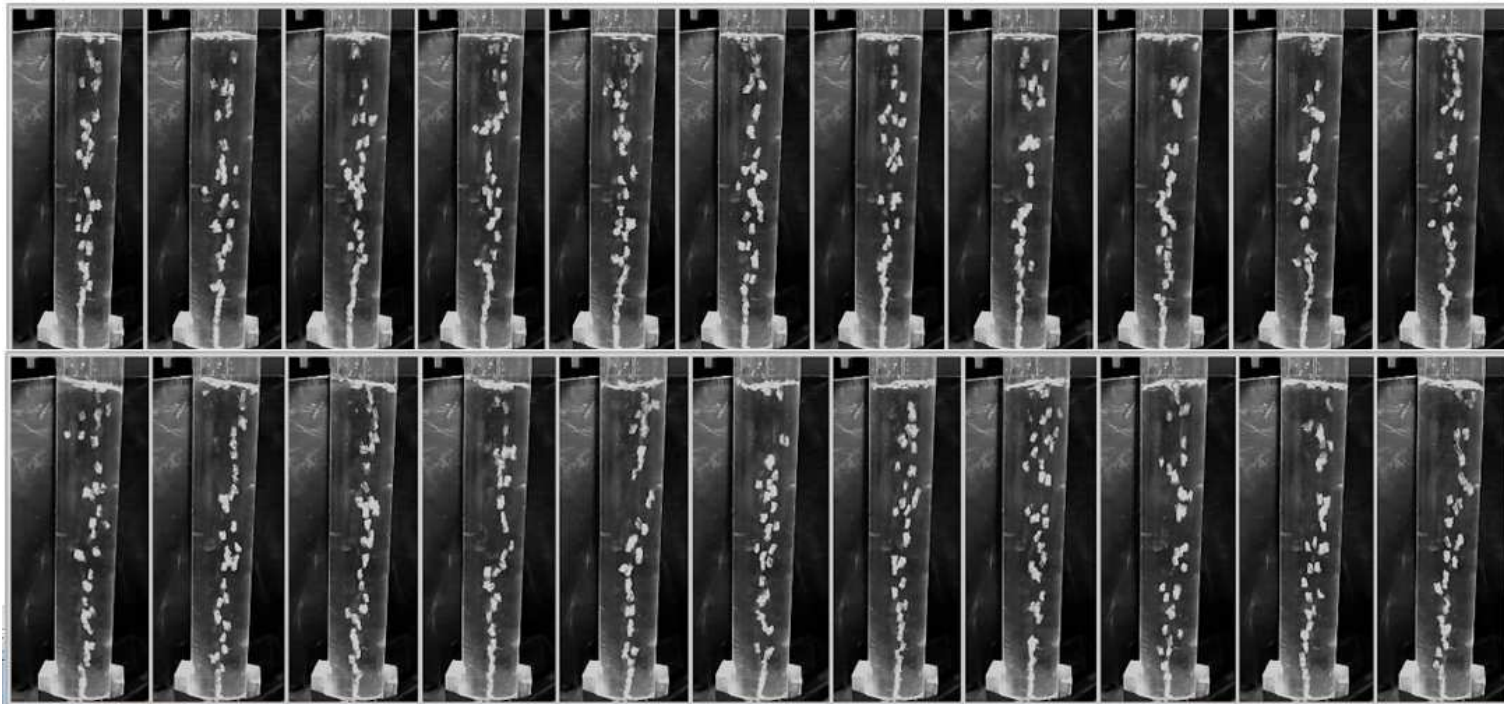


- **Bubble shape** - flexible flat instead of solid sphere  
shape changes while moving

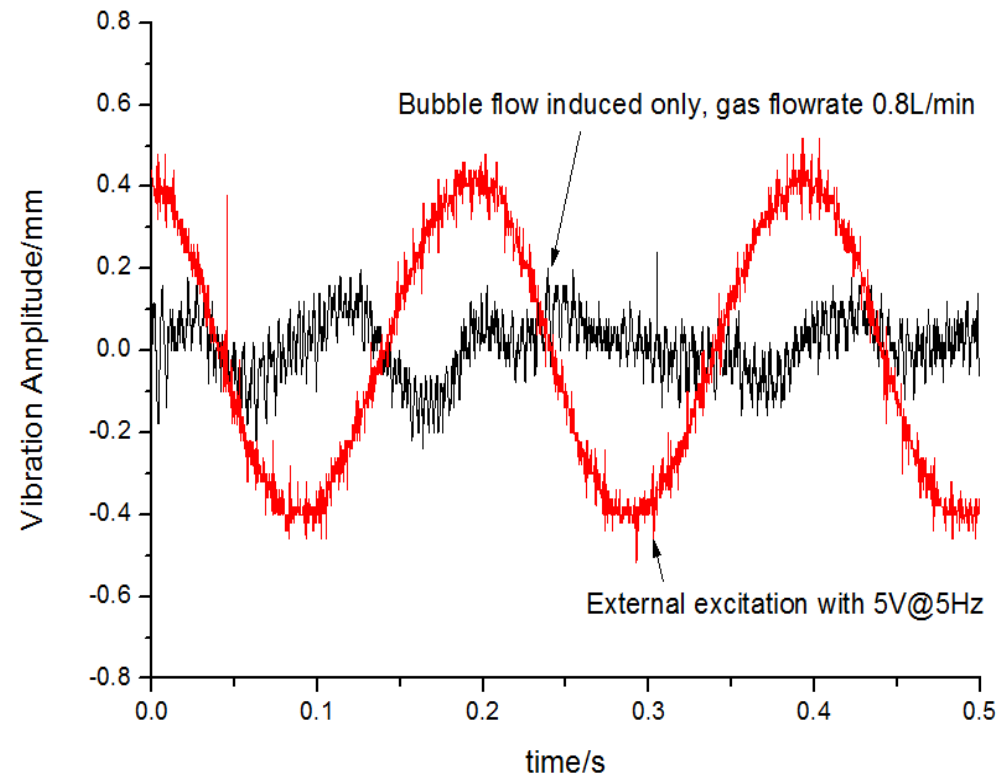




- Bubble motion – spiral instead of straight, caused by flat bubble shape



- bubble induced vibration

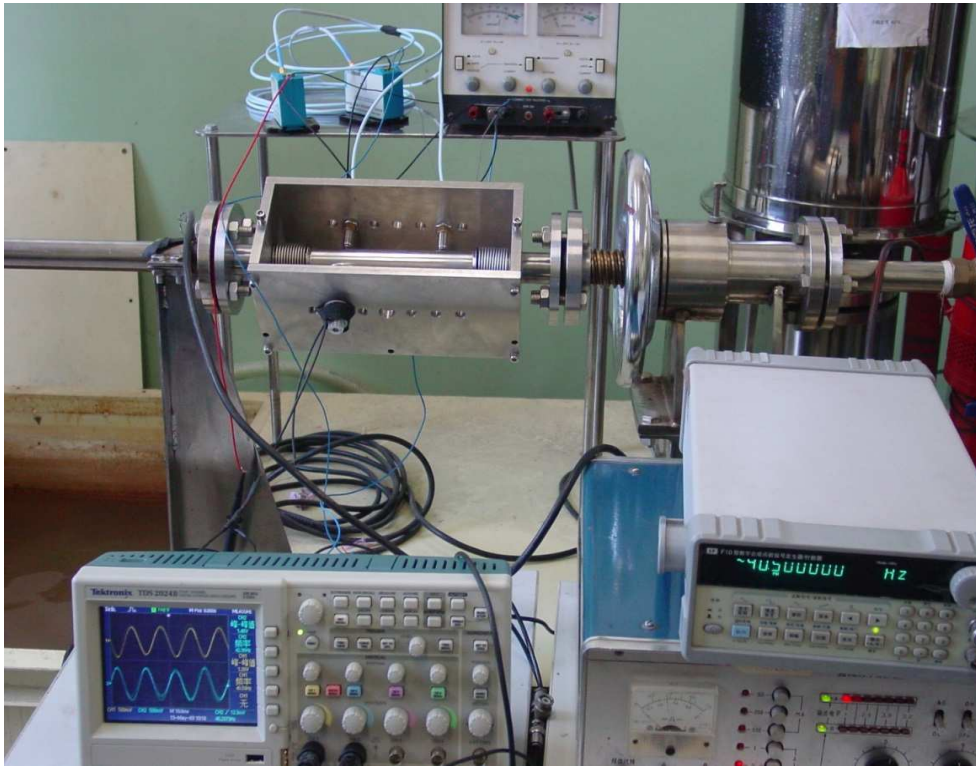


- Standard deviation of bubble flow induced vibration

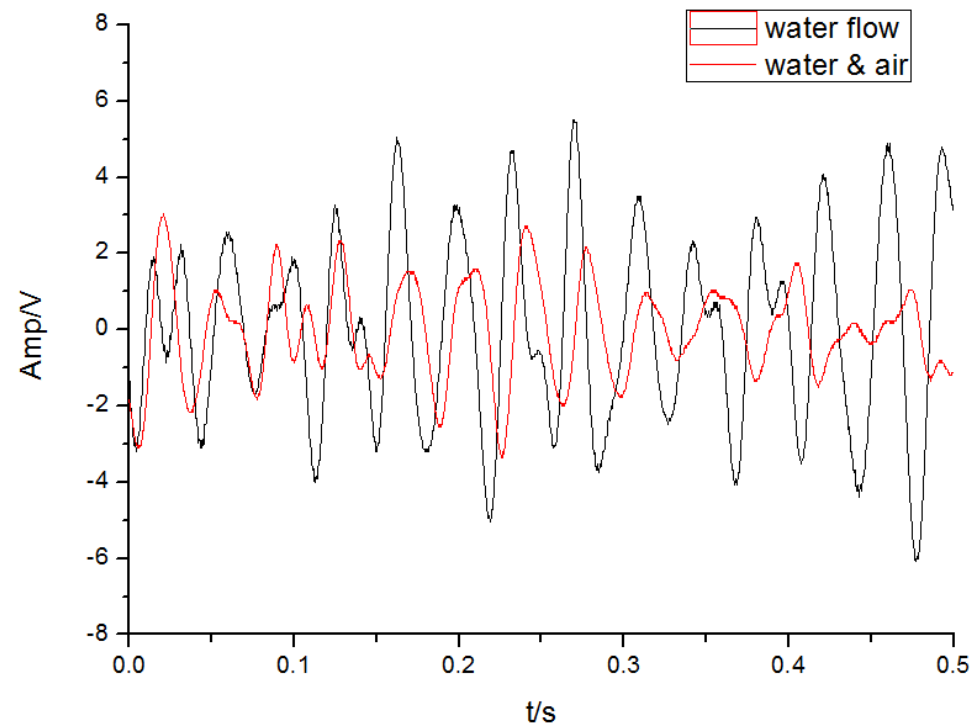
Gas flowrate(L/min)	0.4	0.8	1.2	1.6
Standard deviation with uncertainty	0.053 ±0.003	0.083 ±0.002	0.148 ±0.035	0.235 ±0.067

induced vibration increases with gas void fraction

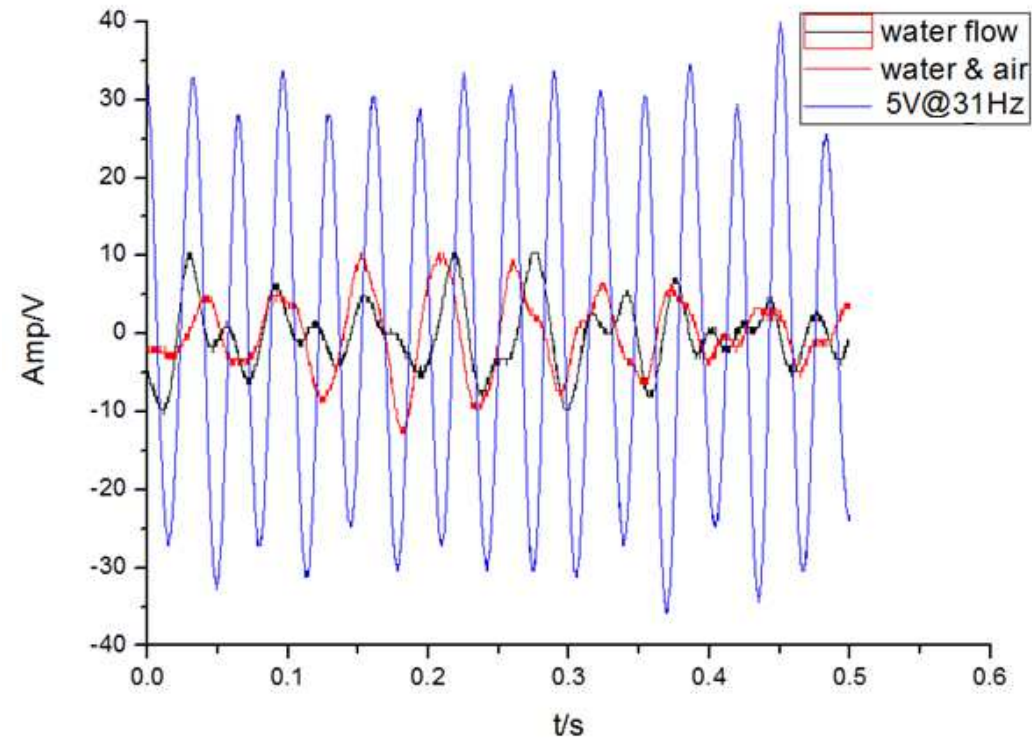
## Experiment - 2: water-air flows



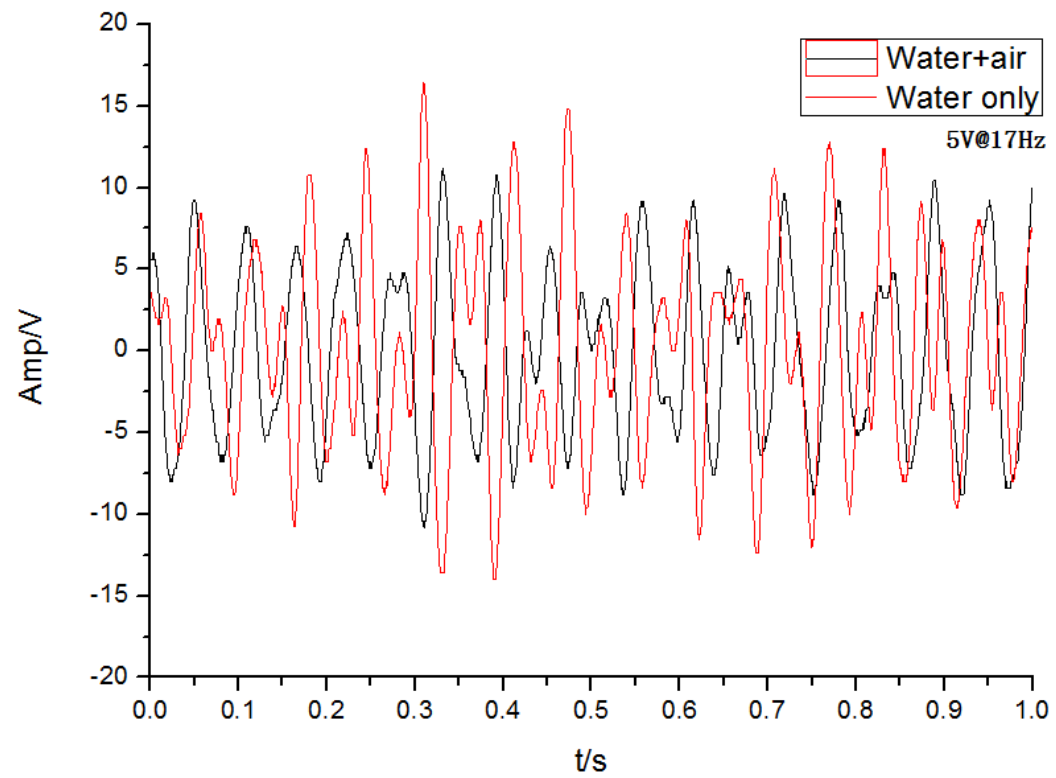
- Flows induced vibration



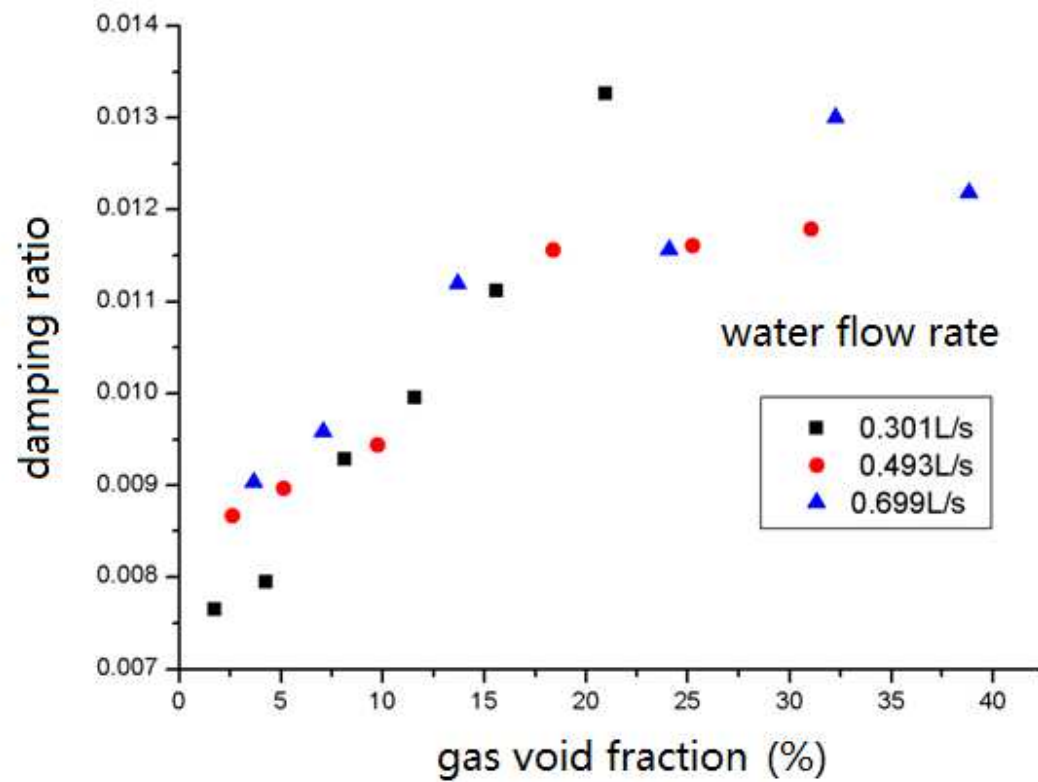
- water flow with/without external vibration



## water flow and water- air flow under external excitation

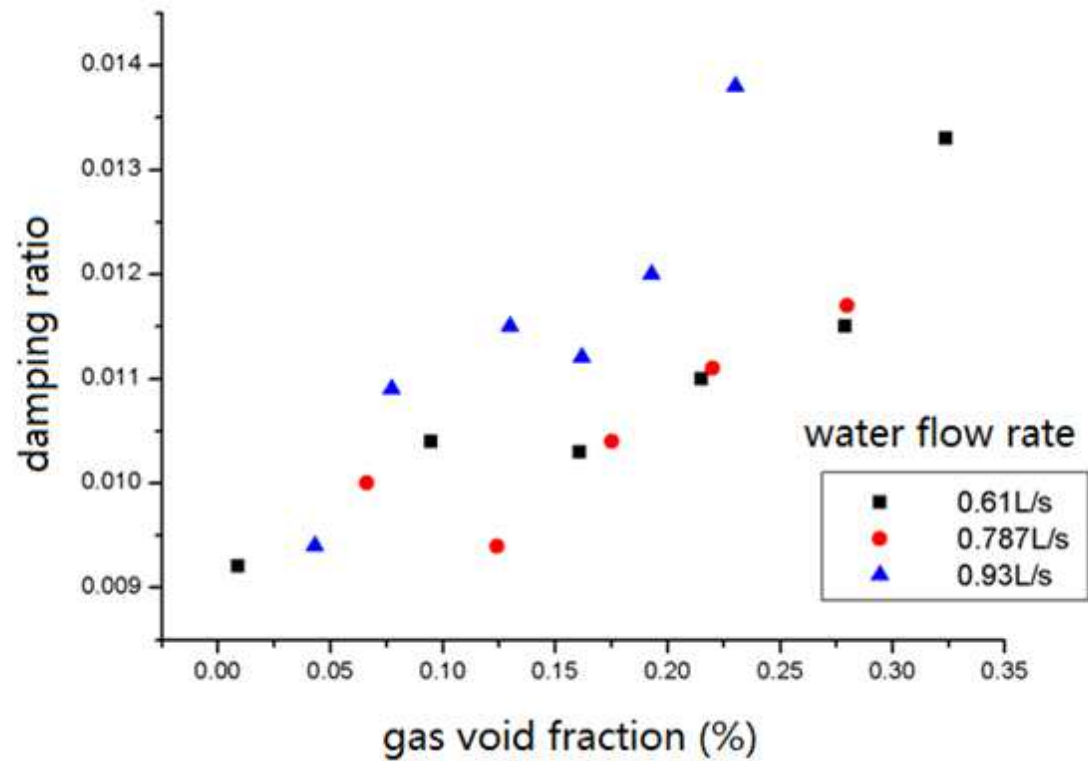


- Water-air flow under vibration – 1st modal damping





- Damping -2<sup>nd</sup> modal



## In modeling

- Transverse vibration of a Coriolis flowmeter in water-air flow may be described by this simplified equation:

$$M \frac{d^2 x}{dt^2} + C \frac{dx}{dt} + Kx = F_0 \sin(\omega t) + F_1 + F_2$$

$M$  - total mass including water and 'added mass' of air;

$C$  - total damping including structure, fluids, phase interaction

$K$  - structure stiffness mainly

$F_0 \sin(\omega t)$  - external excitation

$F_1$  - Coriolis force

$F_2$  - water+ air flows induced transverse force

- almost known    
  - known to some extent    
  - hard to predict

## Bubble shape

- Relative motion/'decouple' makes bubble shape changes. Solid sphere bubble model seems not real. 'Added mass' depends on the shape.
- A flat bubble with added mass coefficient can be up to 0.97. It is larger than 0.5 as given to sphere bubble.
- Unable to give a correct 'added mass' causes error of models.

## Damping of flow ■

- Existence of bubbles in water causes extra vibration damping.
- The damping ratio is proportional to void fraction of the air for both vibration modals (1<sup>st</sup> and 2<sup>nd</sup>)
- Damping suppresses vibration amplitude especially near resonance region, and makes a small shift of resonance frequency.
- Unknown damping may cause error in flowrate measurement

# Bubble motion ■

- Bubbles travel in non-straight way, this induces transverse vibration additional to external excitation, the later is applied by the flowmeter.
- The induced vibration may cause error in flowrate measurement

# flowmeter structure



- Structure of the flowmeter has its intrinsic vibration response property. This is called transfer function.
- Flow induced vibration and external excitation will go through the transfer function to output signal.
- Poor structure design may amplify bubble induced vibration

## Some thing missing?

- Phase distribution and bubble interaction are not considered in above equation.
- They are hard to measure and to describe mathematically. ■

## Possible ways to do improvement

- With good understanding of principles of the meters in multiphase flow:  
Do numerical computation using commercial software for a better design.
- For existing meters:  
Do more measurements ( induced vibration, multi-frequency excitation, additional sensors), then do signal analysis

further work to do



# Summary

- We review works on theoretical models for Coriolis flowmeters used in multiphase flows
- We do experiments on bubble rising in still water and on water-air two-phase flow, with/without external vibration
- It is found:
  - 1) bubbles cannot be taken as solid spheres
  - 2) bubbles moving in water induce transverse vibration
  - 3) bubbles in water induce vibration damping

- Also, difficulties in giving a good model for a Coriolis flow meter in two-phase flow are discussed.
- Further work to improve the theoretical model to reduce measurement errors are suggested.

# References

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**Thank you for your time**  
**obrigado**